Quantum field theory

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Abstract. This is an introduction to quantum field theory and modern particle physics.

Preface

Preface.

Thanks.

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And still on top of this
I'm pretty sure
It must have rained
The day before you came

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There's a place out on the edge of town sir
Rising above the factories and the fields
And ever since I was a child, I can remember
That mansion on the hill

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And all the stars were just like little fish
You should learn when to go
You should learn how to say no

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Frosty wind made moan
Earth stood hard as iron
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Congratulations for having read this book, and no exercises for this final chapter.

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