

The magic of science

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ABSTRACT. This is a general introduction to science, mainly relying on mathematics and physics, and discussing various theoretical and philosophical aspects.

Preface

Preface.

Thanks.

Cergy, January 2025

Teo Banica

Contents

Preface	3
Part I. Math and physics	9
Chapter 1.	11
1a.	11
1b.	11
1c.	11
1d.	11
1e. Exercises	11
Chapter 2.	13
2a.	13
2b.	13
2c.	13
2d.	13
2e. Exercises	13
Chapter 3.	15
3a.	15
3b.	15
3c.	15
3d.	15
3e. Exercises	15
Chapter 4.	17
4a.	17
4b.	17
4c.	17
4d.	17
4e. Exercises	17

Part II. Matter, chemistry	19
Chapter 5.	21
5a.	21
5b.	21
5c.	21
5d.	21
5e. Exercises	21
Chapter 6.	23
6a.	23
6b.	23
6c.	23
6d.	23
6e. Exercises	23
Chapter 7.	25
7a.	25
7b.	25
7c.	25
7d.	25
7e. Exercises	25
Chapter 8.	27
8a.	27
8b.	27
8c.	27
8d.	27
8e. Exercises	27
Part III. Life and biology	29
Chapter 9.	31
9a.	31
9b.	31
9c.	31
9d.	31
9e. Exercises	31

CONTENTS

7

Chapter 10.	33
10a.	33
10b.	33
10c.	33
10d.	33
10e. Exercises	33
Chapter 11.	35
11a.	35
11b.	35
11c.	35
11d.	35
11e. Exercises	35
Chapter 12.	37
12a.	37
12b.	37
12c.	37
12d.	37
12e. Exercises	37
Part IV. Social science	39
Chapter 13.	41
13a.	41
13b.	41
13c.	41
13d.	41
13e. Exercises	41
Chapter 14.	43
14a.	43
14b.	43
14c.	43
14d.	43
14e. Exercises	43
Chapter 15.	45

15a.	45
15b.	45
15c.	45
15d.	45
15e. Exercises	45
Chapter 16.	47
16a.	47
16b.	47
16c.	47
16d.	47
16e. Exercises	47
Bibliography	49

Part I

Math and physics

*Cherish the thought
Of always having you here by my side
Oh baby, I cherish the joy
You keep bringing it into my life*

CHAPTER 1

1a.

1b.

1c.

1d.

1e. Exercises

Exercises:

EXERCISE 1.1.

EXERCISE 1.2.

EXERCISE 1.3.

EXERCISE 1.4.

EXERCISE 1.5.

EXERCISE 1.6.

Bonus exercise.

CHAPTER 2

2a.

2b.

2c.

2d.

2e. Exercises

Exercises:

EXERCISE 2.1.

EXERCISE 2.2.

EXERCISE 2.3.

EXERCISE 2.4.

EXERCISE 2.5.

EXERCISE 2.6.

Bonus exercise.

CHAPTER 3

3a.

3b.

3c.

3d.

3e. Exercises

Exercises:

EXERCISE 3.1.

EXERCISE 3.2.

EXERCISE 3.3.

EXERCISE 3.4.

EXERCISE 3.5.

EXERCISE 3.6.

Bonus exercise.

CHAPTER 4

4a.

4b.

4c.

4d.

4e. Exercises

Exercises:

EXERCISE 4.1.

EXERCISE 4.2.

EXERCISE 4.3.

EXERCISE 4.4.

EXERCISE 4.5.

EXERCISE 4.6.

Bonus exercise.

Part II

Matter, chemistry

*Sonically we're in control
We're the diamond in your soul
Images come thick and fast
From the future, from the past*

CHAPTER 5

5a.

5b.

5c.

5d.

5e. Exercises

Exercises:

EXERCISE 5.1.

EXERCISE 5.2.

EXERCISE 5.3.

EXERCISE 5.4.

EXERCISE 5.5.

EXERCISE 5.6.

Bonus exercise.

CHAPTER 6

6a.

6b.

6c.

6d.

6e. Exercises

Exercises:

EXERCISE 6.1.

EXERCISE 6.2.

EXERCISE 6.3.

EXERCISE 6.4.

EXERCISE 6.5.

EXERCISE 6.6.

Bonus exercise.

CHAPTER 7

7a.

7b.

7c.

7d.

7e. Exercises

Exercises:

EXERCISE 7.1.

EXERCISE 7.2.

EXERCISE 7.3.

EXERCISE 7.4.

EXERCISE 7.5.

EXERCISE 7.6.

Bonus exercise.

CHAPTER 8

8a.

8b.

8c.

8d.

8e. Exercises

Exercises:

EXERCISE 8.1.

EXERCISE 8.2.

EXERCISE 8.3.

EXERCISE 8.4.

EXERCISE 8.5.

EXERCISE 8.6.

Bonus exercise.

Part III

Life and biology

*They say our love
Won't pay the rent
Before it's earned
Our money's always spent*

CHAPTER 9

9a.

9b.

9c.

9d.

9e. Exercises

Exercises:

EXERCISE 9.1.

EXERCISE 9.2.

EXERCISE 9.3.

EXERCISE 9.4.

EXERCISE 9.5.

EXERCISE 9.6.

Bonus exercise.

CHAPTER 10

10a.

10b.

10c.

10d.

10e. Exercises

Exercises:

EXERCISE 10.1.

EXERCISE 10.2.

EXERCISE 10.3.

EXERCISE 10.4.

EXERCISE 10.5.

EXERCISE 10.6.

Bonus exercise.

CHAPTER 11

11a.

11b.

11c.

11d.

11e. Exercises

Exercises:

EXERCISE 11.1.

EXERCISE 11.2.

EXERCISE 11.3.

EXERCISE 11.4.

EXERCISE 11.5.

EXERCISE 11.6.

Bonus exercise.

CHAPTER 12

12a.

12b.

12c.

12d.

12e. Exercises

Exercises:

EXERCISE 12.1.

EXERCISE 12.2.

EXERCISE 12.3.

EXERCISE 12.4.

EXERCISE 12.5.

EXERCISE 12.6.

Bonus exercise.

Part IV

Social science

*My life seems unreal, my crime an illusion
A scene badly written in which I must play
Yet I know as I gaze at my young love beside me
The morning is just a few hours away*

CHAPTER 13

13a.

13b.

13c.

13d.

13e. Exercises

Exercises:

EXERCISE 13.1.

EXERCISE 13.2.

EXERCISE 13.3.

EXERCISE 13.4.

EXERCISE 13.5.

EXERCISE 13.6.

Bonus exercise.

CHAPTER 14

14a.

14b.

14c.

14d.

14e. Exercises

Exercises:

EXERCISE 14.1.

EXERCISE 14.2.

EXERCISE 14.3.

EXERCISE 14.4.

EXERCISE 14.5.

EXERCISE 14.6.

Bonus exercise.

CHAPTER 15

15a.

15b.

15c.

15d.

15e. Exercises

Exercises:

EXERCISE 15.1.

EXERCISE 15.2.

EXERCISE 15.3.

EXERCISE 15.4.

EXERCISE 15.5.

EXERCISE 15.6.

Bonus exercise.

CHAPTER 16

16a.

16b.

16c.

16d.

16e. Exercises

Congratulations for having read this book, and no exercises for this final chapter.

Bibliography

- [1] V.I. Arnold, *Mathematical methods of classical mechanics*, Springer (1974).
- [2] V.I. Arnold, *Lectures on partial differential equations*, Springer (1997).
- [3] M.F. Atiyah, *The geometry and physics of knots*, Cambridge Univ. Press (1990).
- [4] T. Banica, *Introduction to modern physics* (2024).
- [5] T. Banica, *The story of particle physics* (2024).
- [6] R.J. Baxter, *Exactly solved models in statistical mechanics*, Academic Press (1982).
- [7] S.M. Carroll, *Spacetime and geometry*, Cambridge Univ. Press (2004).
- [8] D.D. Clayton, *Principles of stellar evolution and nucleosynthesis*, Univ. of Chicago Press (1968).
- [9] A. Connes, *Noncommutative geometry*, Academic Press (1994).
- [10] W.N. Cottingham and D.A. Greenwood, *An introduction to the standard model of particle physics*, Cambridge Univ. Press (2012).
- [11] P.A. Davidson, *Introduction to magnetohydrodynamics*, Cambridge Univ. Press (2001).
- [12] P. Di Francesco, P. Mathieu and D. Sénéchal, *Conformal field theory*, Springer (1996).
- [13] P.A.M. Dirac, *Principles of quantum mechanics*, Oxford Univ. Press (1930).
- [14] S. Dodelson, *Modern cosmology*, Academic Press (2003).
- [15] A. Einstein, *Relativity: the special and the general theory*, Dover (1916).
- [16] L.C. Evans, *Partial differential equations*, AMS (1998).
- [17] L.D. Faddeev and L. A. Takhtajan, *Hamiltonian methods in the theory of solitons*, Springer (2007).
- [18] E. Fermi, *Thermodynamics*, Dover (1937).
- [19] R.P. Feynman, R.B. Leighton and M. Sands, *The Feynman lectures on physics I: mainly mechanics, radiation and heat*, Caltech (1963).
- [20] R.P. Feynman, R.B. Leighton and M. Sands, *The Feynman lectures on physics II: mainly electromagnetism and matter*, Caltech (1964).
- [21] R.P. Feynman, R.B. Leighton and M. Sands, *The Feynman lectures on physics III: quantum mechanics*, Caltech (1966).
- [22] R.P. Feynman and A.R. Hibbs, *Quantum mechanics and path integrals*, Dover (1965).
- [23] A.P. French, *Special relativity*, Taylor and Francis (1968).
- [24] N. Goldenfeld, *Lectures on phase transitions and the renormalization group*, CRC Press (1992).

- [25] H. Goldstein, C. Safko and J. Poole, *Classical mechanics*, Addison-Wesley (1980).
- [26] M.B. Green, J.H. Schwarz and E. Witten, *Superstring theory*, Cambridge Univ. Press (2012).
- [27] D.J. Griffiths, *Introduction to electrodynamics*, Cambridge Univ. Press (2017).
- [28] D.J. Griffiths and D.F. Schroeter, *Introduction to quantum mechanics*, Cambridge Univ. Press (2018).
- [29] D.J. Griffiths, *Introduction to elementary particles*, Wiley (2020).
- [30] K. Huang, *Quantum field theory*, Wiley (1998).
- [31] K. Huang, *Quarks, leptons and gauge fields*, World Scientific (1982).
- [32] C. Itzykson and J.B. Zuber, *Quantum field theory*, Dover (1980).
- [33] L.P. Kadanoff, *Statistical physics: statics, dynamics and renormalization*, World Scientific (2000).
- [34] T. Kibble and F.H. Berkshire, *Classical mechanics*, Imperial College Press (1966).
- [35] M. Kumar, *Quantum: Einstein, Bohr, and the great debate about the nature of reality*, Norton (2009).
- [36] T. Lancaster and K.M. Blundell, *Quantum field theory for the gifted amateur*, Oxford Univ. Press (2014).
- [37] L.D. Landau and E.M. Lifshitz, *Mechanics*, Pergamon Press (1960).
- [38] L.D. Landau and E.M. Lifshitz, *The classical theory of fields*, Addison-Wesley (1951).
- [39] L.D. Landau and E.M. Lifshitz, *Quantum mechanics: non-relativistic theory*, Pergamon Press (1959).
- [40] V.B. Berestetskii, E.M. Lifshitz and L.P. Pitaevskii, *Quantum electrodynamics*, Butterworth-Heinemann (1982).
- [41] R.K. Pathria and P.D. Beale, *Statistical mechanics*, Elsevier (1972).
- [42] M. Peskin and D.V. Schroeder, *An introduction to quantum field theory*, CRC Press (1995).
- [43] M. Schwartz, *Principles of electrodynamics*, Dover (1972).
- [44] J. Schwinger, L.L. DeRaad Jr., K.A. Milton and W.Y. Tsai, *Classical electrodynamics*, CRC Press (1998).
- [45] J. Schwinger and B.H. Englert, *Quantum mechanics: symbolism of atomic measurements*, Springer (2001).
- [46] J.R. Taylor, *Classical mechanics*, Univ. Science Books (2003).
- [47] J. von Neumann, *Mathematical foundations of quantum mechanics*, Princeton Univ. Press (1955).
- [48] S. Weinberg, *Foundations of modern physics*, Cambridge Univ. Press (2011).
- [49] S. Weinberg, *Lectures on quantum mechanics*, Cambridge Univ. Press (2012).
- [50] S. Weinberg, *Lectures on astrophysics*, Cambridge Univ. Press (2019).